Library lecture_tactics_long_version

Lecture 4: Tactics in UniMath

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This is the extended version of a presentation at the UniMath school 2017 in Birmingham, meant for self-study and for exploring the UniMath library.

The material has been slightly enriched on December 13, 2017, which is one day after the presentation.

Compiles with the command coqc -type-in-type lecture_tactics_long_version.v

when placed into the UniMath library

Can be transformed into HTML documentation with the command coqdoc -utf8 lecture_tactics_long_version.v

In Coq, one can define concepts by directly giving well-typed terms, but one can also be helped in the construction by the interactive mode.

Require Import UniMath.Foundations.Preamble.

define a concept interactively:

Locate bool.

bool comes from the Coq library

Definition myfirsttruthvalue: bool.

only the identifier and its type given, not the definiens

This opens the interactive mode.

The UniMath style guide asks us to start what follows with Proof. in a separate line. In vanilla Coq, this would be optional (it is anyway a "nop").

Proof.

Now we still have to give the term, but we are in interactive mode. If you want to see everything that *involves* booleans, then do

Search bool.

If you think there are too many hits and you only want to find library elements that *yield* booleans, then try

SearchPattern bool.

If you want to see everything that *involves* booleans, then try

Search bool.

true does not take an argument, and it is already a term we can take as definiens.

exact true.

exact is a tactic which takes the term as argument and informs Coq in the proof mode to finish the current goal with that term.

We see in the response buffer: "No more subgoals." Hence, there is nothing more to do, except for leaving the proof mode properly.

Defined.

Defined. instructs Coq to complete the whole interactive construction of a term, verify it and to associate it with the given identifer, here myfirsttruthvalue.

Search bool.

The new definition appears at the end of the list.

Print myfirsttruthvalue.

a more compelling example

```
Definition mysecondtruthvalue: bool.
Proof.
    Search bool.
    apply negb.
```
applies the function negb to obtain the required boolean, thus the system has to ask for its argument

```
exact myfirsttruthvalue.
Defined.
```
Print mysecondtruthvalue.

```
mysecondtruthvalue = negb myfirsttruthvalue
          : bool
```
the definition is "as is", evaluation can be done subsequently:

```
Eval compute in mysecondtruthvalue.
```

```
     = false
     : bool
```
Again, not much has been gained by the interactive mode.

```
Definition mythirdtruthvalue: bool.
Proof.
    Search bool.
    apply andb.
```
apply andb. applies the function andb to obtain the required boolean, thus the system has to ask for its TWO arguments, one by one

This follows the proof pattern of "backward chaining" that tries to attack goals instead of building up evidence. In the course of action, more goals can be generated. The proof effort is over when no more goal remains.

UniMath coding style asks you to use proof structuring syntax, while vanilla Coq would allow you to write formally verified "spaghetti code".

We tell Coq that we start working on the first subgoal.

only the "focused" subgoal is now on display

```
    apply andb.
```
this again spawns two subgoals

```
we tell Coq that we start working on the first subgoal
```
+

-

normally, one would not leave the "bullet symbol" isolated in a line

```
      exact mysecondtruthvalue.
    + exact myfirsttruthvalue.
```
The response buffer signals:

```
This subproof is complete, but there are some unfocused goals.
                                        Focus next goal with bullet -.
```

```
  - exact true.
Defined.
```
The usual "UniMath bullet order" is $-$, $+$, $*$, $-$, $+$, $*$, $-$, $-$, $+$, $*$, $*$, and so on (all the ones shown are being used).

Coq does not impose any order, so one can start with, e.g., *****, if need be for the sake of experimenting with a proof.

Reuse of bullets even on one branch is possible by enclosing subproofs in curly braces {}.

```
Print mythirdtruthvalue.
Eval compute in mythirdtruthvalue.
```
You only saw the tactics exact and apply at work, and there was no context.

doing Curry-Howard logic

Interactive mode is more wide-spread when it comes to carrying out proofs (the command Proof. is reminiscent of that).

Disclaimer: this section has a logical flavour, but the "connectives" are not confined to the world of propositional or predicate logic. In particular, there is no reference to the sort Prop of Coq. Prop is not used at all in UniMath!

On first reading, it is useful to focus on the logical meaning.

```
Locate "->".
```
non-dependent product, can be seen as implication

```
Locate "∅".
Print Empty_set.
```
an inductive type that has no constructor

```
Locate "¬".
```
Require Import UniMath.Foundations.PartA.

Do not write the import statements in the middle of a vernacular file. Here, it is done to show the order of appearance, but this is only for reasons of pedagogy.

```
Locate -".
Print neg.
```
Negation is not a native concept; it is reduced to implication, as is usual in constructive logic.

```
Locate "×".
Print dirprod.
```
non-dependent sum, can be seen as conjunction

```
Definition combinatorS (A B C: UU): (A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C.
Proof.
```
how to infer an implication?

 intro Hyp123. set (Hyp $1 := pr1$ Hyp 123).

This is already a bit of "forward chaining" which is a fact-building process.

```
set (Hyp23 := pr2 Hyp123).
  cbn in Hyp23.
```
cbn simplifies a goal, and cbn in H does this for hypothesis H; note that simpl has the same high-level description but should better be avoided in new developments.

```
set (Hyp2 := pr1 Hyp23).
set (Hyp3 := pr2 Hyp23).
  cbn in Hyp3.
  apply Hyp1.
  apply tpair.
```
could be done with split. as well

- assumption.

instruct Coq to look into the current context

this could be done with exact Hyp3. as well

```
  - apply Hyp2.
         assumption.
Defined.
Print combinatorS.
Local Definition combinatorS intro pattern (A B C: UU):
  (A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C.
Proof.
    intros [Hyp1 [Hyp2 Hyp3]].
```
deconstruct the hypothesis at the time of introduction; notice that \times associates to the right; intros can also introduce multiple hypotheses, see below

 apply Hyp1. split.

```
  - assumption.
    - apply Hyp2.
        assumption.
Defined.
```
Print combinatorS intro pattern.

may look harmless but is not allowed by UniMath coding style

```
Set Printing All.
Print combinatorS_intro_pattern.
```
UniMath coding style forbids the generation of terms that involve match constructs! The UniMath language is a voluntarily limited subset of Coq, and tactics need to be used with care so as to stay within that fragment.

```
Unset Printing All.
```
However, the two definitions are even convertible:

```
Local Lemma combinatorS_intro_pattern_is_the_same:
    combinatorS = combinatorS_intro_pattern.
Proof.
    apply idpath.
Defined.
```
another try to make life easier:

```
Local Definition combinatorS_destruct (A B C: UU):
  (A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C.
Proof.
    intro Hyp123.
  destruct Hyp123 as [Hyp1 Hyp23].
```
deconstruct the hypothesis when needed

 apply Hyp1. destruct Hyp23 as [Hyp2 Hyp3].

deconstruct the hypothesis when needed

```
  split.
    - assumption.
    - apply Hyp2.
        assumption.
Defined.
Set Printing All.
Print combinatorS destruct.
```

```
Unset Printing All.
```
Since we see match, this proof is therefore equally disallowed by UniMath coding style!

Again, the definition is definitionally equal to the first one:

```
Local Lemma combinatorS_destruct_is_the_same: combinatorS = combinatorS_destruct.
Proof.
   apply idpath.
Defined.
```
We declared the unwanted definitions and lemmas as Local, so that they would at least not be exported. In the UniMath library, there should be no such definitions at all, not even declared as local.

The way out:

```
Definition combinatorS induction (A B C: UU): (A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C.
Proof.
    intro Hyp123.
    induction Hyp123 as [Hyp1 Hyp23].
 wishes to invoke the recursor
    apply Hyp1.
    induction Hyp23 as [Hyp2 Hyp3].
 wishes to invoke the recursor
    split.
    - assumption.
    - apply Hyp2.
        assumption.
```
Defined.

Set Printing All. Print combinatorS induction. Unset Printing All.

Unfortunately, this is not better than before, but it comes from a recent change in the status of Sigma types. They are a record now, in order to profit from "primitive projections". The UniMath team would hope that the Coq developers provide a means of inducing Coq into using the induction principle total2_rect when calling tactic induction on Sigma types and their special case that is pairs.

Notice that even the projections pr1 and pr2 are defined by help of match - for the time being, since this is what happens with non-recursive fields of Coq records.

```
Definition combinatorS_curried (A B C: UU): (A \rightarrow B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow A \rightarrow C.
Proof.
```
use intro three times or rather intros once; UniMath coding style asks for giving names to all hypotheses that are not already present in the goal

formula, see also the next definition

```
  intros H1 H2 H3.
  apply H1.
  - assumption.
- set (proofofB := H2 H3).
```
set up abbreviations that can make use of the current context; will be considered as an extra element of the context:

```
    assumption.
Defined.
```
Print combinatorS curried.

We see that set gives rise to let-expressions that are known from functional programming languages, in other words: the use of set is not a "macro" facility to ease typing.

let-bindings disappear when computing the normal form of a term:

Compute combinatorS_curried.

set can only be used if the term of the desired type is provided, but we can also work interactively as follows:

```
Definition combinatorS curried with assert (A B C: UU):
   (A \rightarrow B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow A \rightarrow C.
Proof.
     intros H1 H2 H3.
```
we can momentarily forget about our goal and build up knowledge:

```
  assert (proofofB : B).
```
the current goal C becomes the second sub-goal, and the new current goal is B

It is not wise to handle this situation by "bullets" since many assertions can appear in a linearly thought argument. It would pretend a tree structure although it would rather be a comb. The proof of the assertion should be packaged by enclosing it in curly braces like so:

```
  { apply H2.
      assumption.
  }
```
Now, proofofB is in the context with type B.

```
  apply H1.
    - assumption.
    - assumption.
Defined.
```
the wildcard ? for intros

```
Definition combinatorS curried variant (A B C: UU):
   (A \rightarrow B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow \forall H7:A, C.
Proof.
    intros H1 H2 ?.
```
a question mark instructs Coq to use the corresponding identifier from the goal formula

```
  exact (H1 H7 (H2 H7)).
Defined.
```
the wildcard _ for intros forgets the respective hypothesis

Locate "⨿".

this symbol is harder to type in with Agda input mode: use backslash union and then choose the right symbol with arrow down key: the symbol might only appear in the menu to choose from after having hit the arrow down key!

Print coprod.

defined in UniMath preamble as inductive type, can be seen as disjunction

Locate "∏".

company-coq shows the result with universal quantifiers, but that is only the "prettified" version of "forall" which is a basic syntactic element of the language of Coq.

 $Locate = "$.

the identity type of UniMath

Print paths.

A word of warning for those who read "Coq in a Hurry": SearchRewrite does not find equations w.r.t. this notion, only w.r.t. Coq's built-in propositional equality.

SearchPattern (paths).

Among the search results is pathsinv0l that has idpath in its conclusion.

SearchRewrite idpath.

No result!

How to decompose formulas

In "Coq in a Hurry", Yves Bertot gives recipes for decomposing the usual logical connectives. Crucially, one has to distinguish between decomposition of the goal or decomposition of a hypothesis in the context.

Here, we do it alike.

Decomposition of goal formulas:

A1,...,An -> B: tactic intro or intros

 \neg A: idem (negation is defined through implication)

Π-type: idem (implication is a special case of product)

×: apply dirprodpair, less specifically apply tpair or split

Σ-type: use tpair or ∃ or split with, see explanations below

A II B: apply ii1 or apply ii2, but this constitutes a choice of which way to go

 $A = B$: apply idpath, however this only works when the expressions are convertible

nat: exact 2017, for example (a logical reading is not useful for this type)

Decomposition of formula of hypothesis H:

∅: induction H

This terminates a goal. (It corresponds to ex falso quodlibet.)

There is naturally no recipe for getting rid of \varnothing in the conclusion. But apply fromempty allows to replace any goal by ∅.

A1,...,An -> B: apply H, but the formula has to fit with the goal

×: induction H as [H1 H2]

As seen above, this introduces names of hypotheses for the two components.

 $Σ$ -type: idem, but rather more asymmetric as induction H as [x H']

A ⨿ B: induction H as [H1 | H2]

This introduces names for the hypotheses in the two branches.

 $A = B$: induction H

The supposedly equal A and B become the same A in the goal.

This is the least intuitive rule for the non-expert in type theory.

```
nat: induction n as [ | n IH]
```
Here, we assume that the hypothesis has the name n which is more idiomatic than H, and there is no extra name in the base case, while in the step case, the preceding number is now given the name n and the induction hypothesis is named IH.

Handling unfinished proofs

In the middle of a proof effort - not in the UniMath library - you can use admit to abandon the current goal.

```
Local Lemma badex1 (A: UU): \varnothing \times (A \rightarrow A).
Proof.
    split.
  -
```
seems difficult in the current context

admit.

we continue with decent proof work:

```
  - intro H.
        assumption.
Admitted.
```
This is strictly forbidden to commit to UniMath! admit allows to pursue the other goals, while Admitted. makes the lemma available for further proofs.

An alternative to interrupt work on a proof:

```
Lemma badex2 (A: UU): \varnothing \times (A → A).
Proof.
    split.
```
 - Abort.

badex2 is not in the symbol table.

Abort. is a way of documenting a problem with proving a result. At least, Coq can check the partial proof up to the Abort. command.

Working with holes in proofs

Our previous proofs were particularly clear because the goal formulas and all hypotheses were fully given by the system.

Print pathscomp0.

This is the UniMath proof of transitivity of equality.

The salient feature of transitivity is that the intermediate expression cannot be deduced from the equation to be proven.

```
Lemma badex3 (A B C D: UU) : ((A \times B) \times (C \times D)) = (A \times (B \times C) \times D).
```
Notice that the outermost parentheses are needed here.

```
Proof.
    Fail apply pathscomp0.
```

```
The command has indeed failed with message:
Cannot infer the implicit parameter b of pathscomp0 whose type is
"Type" in environment:
A, B, C, D : UU
```
(When using the standard setup of UniMath with ProofGeneral, this message appears only when starting emacs at the root of the UniMath library.)

Fail announces failure and therefore allows to continue with the interpretation of the vernacular file.

We need to help Coq with the argument b to pathscomp0.

```
apply (pathscomp\theta (b := A × (B × (C × D)))).
```
is this not just associativity with third argument $C \times D$?

```
SearchPattern( \times ).
```
No hope at all - we can only hope for weak equivalence.

Abort.

-

```
SearchPattern(\geq \geq \geq).
Print weqcomp.
Print weqdirprodasstor.
Print weqdirprodasstol.
Print weqdirprodf.
Print idweq.
Lemma assocex (A B C D: UU) : ((A \times B) \times (C \times D)) \approx (A \times (B \times C) \times D).
Proof.
    Fail apply weqcomp.
    eapply weqcomp.
```
eapply generates "existential variables" for the expressions it cannot infer from applying a lemma.

The further proof will narrow on those variables and finally make them

-

disappear - otherwise, the proof is not considered completed.

We recall that on this side, only associativity was missing.

 apply weqdirprodasstor. -

The subgoal is now fully given.

The missing link is associativity, but only on the right-hand side of the top \times symbol.

```
    apply weqdirprodf.
        + apply idweq.
        + apply weqdirprodasstol.
Defined.
```
Warning: tactic exact does not work if there are existential variables in the goal, but eexact can then be tried.

```
Lemma sumex (A: UU) (P Q: A \rightarrow UU):
  (\sum x:A, P x \times Q x) \rightarrow (\sum x:A, P x) \times \sum x:A, Q x.Proof.
 decompose the implication:
    intro H.
 decompose the Σ-type:
    induction H as [x H'].
 decompose the pair:
    induction H' as [H1 H2].
 decompose the pair in the goal
    split.
    - Fail split.
 The command has indeed failed with message:
                     Unable to find an instance for the variable pr1.
        Fail (apply tpair).
 A simple way out, by providing the first component:
        split with x.
 ∃ x does the same
        assumption.
```
-

or use eapply and create an existential variable:

```
    eapply tpair.
    Fail assumption.
```
the assumption H2 does not agree with the goal

```
    eexact H2.
Defined.
```
Notice that eapply tpair is not used in the UniMath library, since use tpair normally comes in handier, see below.

Warning on existential variables

It may happen that the process of instantiating existential variables is not completed when all goals have been treated.

an example adapted from one by Arnaud Spiwack, ~2007

```
About unit.
```
from the Coq library

```
Local Definition P (x:nat) := unit.
```

```
Lemma uninstex: unit.
Proof.
 refine ((fun x:P = |P|).
```
refine is like exact, but one can leave holes with the wildcard "_". This tactic should hardly be needed since most uses in UniMath can be replaced by a use of the "tactic" use, see further down on this tactic notation for an Ltac definition.

Still, refine can come to rescue in difficult situations, in particular during proof development. Its simpler variant simple refine is captured by the use "tactic".

```
  - exact tt.
  - exact tt.
```
Now, Coq presents a subgoal that pops up from the "shelved goals".

Still, no more "-" bullets can be used.

```
[ - Error: Wrong bullet - : No more subgoals. ]
```
Show Existentials.

a natural number is still asked for

Unshelve.

Like this, we can focus on the remaining goal.

exact 0. Defined.

one can also name the existential variables in refine:

```
Lemma uninstexnamed: unit.
    Proof.
    refine ((fun x:P ?[n] \Rightarrow ) ).
```
give a name to the existential variable

```
    - exact tt.
        - exact tt.
Show Existentials.
Unshelve.
instantiate (n := 0).
```
more symbols to type but better to grasp

Defined.

a bit more on equational reasoning

Section homot.

A section allows to introduce local variables/parameters that will be bound outside of the section.

Locate $~\sim$ ".

Print homot.

this is just pointwise equality

Print idfun.

the identity function

Locate "∘". Print funcomp.

plain function composition in diagrammatic order, i.e., first the first argument, then the second argument; the second argument may even have a dependent type

```
Variables A B: UU.
Definition interestingstatement : UU :=
 \Box (v w : A → B) (v' w' : B → A),
```
w ∘ w' ~ idfun B → v' ∘ v ~ idfun A → v' ~ w' → v ~ w.

Check (isinjinvmap': interestingstatement).

```
Lemma ourisinjinvmap': interestingstatement.
Proof.
```
intros.

is a nop since the formula structure is not analyzed

```
  unfold interestingstatement.
```
unfold unfolds a definition

intros ? ? ? ? homoth1 homoth2 hyp a.

the extra element a triggers Coq to unfold the formula further; unfold interestingstatement was there only for illustration!

we want to use transitivity that is expressed by pathscomp0 and instruct Coq to take a specific intermediate term

```
Set Printing All.
Print Ltac intermediate path.
```
reveals that there is an abbreviation for the tactic call we have in mind

```
Unset Printing All.
  intermediate path (w (w' (v a))).
    - apply pathsinv0.
```
apply symmetry of equality

```
    unfold homot in homoth1.
    unfold funcomp in homoth1.
    unfold idfun in homoth1.
    apply homoth1.
```
all the unfold were only for illustration!

```
    Print maponpaths.
    apply maponpaths.
    unfold homot in hyp.
```
we use the equation in hyp from right to left, i.e., backwards:

rewrite <- hyp.

remark: for a forward rewrite, use rewrite without directional argument beautify the current goal:

change $((v' \circ v) a = idfun A a)$.

just for illustration of change that allows to replace the goal by a convertible expression; also works for hypotheses, e.g.:

change $(v' - w')$ in hyp.

-

since hyp was no longer necessary, we should rather have deleted it:

```
    clear hyp.
        apply homoth2.
Defined.
Variables v w: A \rightarrow B.
Variables v' w': B \rightarrow A.
Eval compute in (ourisinjinvmap' v w v' w').
Opaque ourisinjinvmap'.
Eval compute in (ourisinjinvmap' v w v' w').
```
Opaque made the definition opaque in the sense that the identifier is still in the symbol table, together with its type, but that it does not evaluate to anything but itself.

If inhabitants of a type are irrelevant (for example if it is known that there is at most one inhabitant, and if one therefore is not interested in computing with that inhabitant), then opaqueness is an asset to make the subsequent proof process lighter.

Opaque can be undone with Transparent:

```
Transparent ourisinjinvmap'.
Eval compute in (ourisinjinvmap' v w v' w').
```
Full and irreversible opaqueness is obtained for a construction in interactive mode by completing it with Qed. in place of Defined.

Using Qed. is discouraged by the UniMath style guide. In Coq, most lemmas, theorems, etc. (nearly every assertion in Prop) are made opaque in this way. In UniMath, many lemmas enter subsequent computation, and one should have good reasons for not closing an interactive construction with Defined.

```
End homot.
Check ourisinjinvmap'.
```
The section variables A and B are abstracted away after the end of the section - only the relevant ones.

assert is a "chameleon" w.r.t. to opaqueness:

```
Definition combinatorS curried with assert2 (A B C: UU):
   (A \rightarrow B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow A \rightarrow C.
Proof.
    intros H1 H2 H3.
    assert (proofofB : B).
    { apply H2.
         assumption.
```
}

proofofB is just an identifier and not associated to the construction we gave. Hence, the proof is opaque for us.

```
  apply H1.
    - assumption.
    - assumption.
Defined.
Print combinatorS curried with assert2.
```
We see that proofofB is there with its definition, so it is transparent.

See much further below for transparent assert that is like assert, but consistently transparent.

composing tactics

Up to now, we "composed" tactics in two ways: we gave them sequentially, separated by periods, or we introduced a tree structure through the "bullet" notation. We did not think of these operations as composition of tactics, in particular since we had to trigger each of them separately in interactive mode. However, we can also explicitly compose them, like so:

```
Definition combinatorS induction in one step (A B C: UU):
  (A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C.
Proof.
    intro Hyp123;
    induction Hyp123 as [Hyp1 Hyp23];
    apply Hyp1;
    induction Hyp23 as [Hyp2 Hyp3];
    split;
    [ assumption
    | apply Hyp2;
         assumption].
Defined.
```
The sequential composition is written by (infix) semicolon, and the two branches created by split are treated in the |-separated list of arguments to the brackets.

Why would we want to do such compositions? There are at least four good reasons:

(1) We indicate that the intermediate results are irrelevant for someone who executes the script so as to understand how and why the construction / the proof works.

(2) The same tactic (expression) can uniformly treat all sub-goals stemming

from the preceding tactic application, as will be shown next.

```
Definition combinatorS curried with assert in one step (A B C: UU):
   (A \rightarrow B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow A \rightarrow C.
Proof.
    intros H1 H2 H3;
    assert (proofofB : B) by
     ( apply H2;
        assumption
    );
    apply H1;
    assumption.
Defined.
```
This illustrates the grouping of tactic expressions by parentheses, the variant assert by of assert used when only one tactic expression forms the proof of the assertion, and also point (2): the last line is simpler than the expected line [assumption | assumption].

Why would we want to do such compositions (cont'd)?

(3) We want to capture recurring patterns of construction / proof by tactics into reusable Ltac definitions, see below.

(4) We want to make use of the abstract facility, explained now.

```
Definition combinatorS induction with abstract (A B C: UU):
  (A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C.
Proof.
    intro Hyp123;
    induction Hyp123 as [Hyp1 Hyp23];
    apply Hyp1;
    induction Hyp23 as [Hyp2 Hyp3].
```
Now imagine that the following proof was very complicated but had no computational relevance, i.e., could also be packed into a lemma whose proof would be finished by Qed. We can encapsulate it into abstract:

```
  abstract (split;
    [ assumption
    | apply Hyp2;
        assumption]).
Defined.
```
Print combinatorS induction with abstract.

The term features an occurrence of combinatorS_induction_with_abstract_subproof that contains the abstracted part; using the latter name is forbidden by the UniMath style guide. Note that abstract is used hundreds of times in the UniMath library.

Ltac language for defining tactics

Disclaimer: Ltac can more than that, in fact Ltac is the name of the whole tactic language of Coq.

Ltac definitions can associate identifiers for tactics with tactic expressions.

We have already used one such identifier: intermediate_path in the Foundations package of UniMath. In file PartA.v, we have the code Ltac intermediate path $x := apply (pathscomp0 (b := x)).$

Print Ltac intermediate path.

does not show the formal argument x in the right-hand side. Remedy:

```
Set Printing All.
Print Ltac intermediate path.
Unset Printing All.
```
The problem with these Ltac definitions is that they are barely typed, they behave rather like LaTeX macros.

```
Ltac intermediate path wrong x := apply (pathscomp0 (X := x)(b := x)).
```
This definition confounds the type argument X and its element b . The soundness of Coq is not at stake here, but the errors only appear at runtime.

```
Section homot2.
Variables A B: UU.
Lemma ourisinjinvmap' failed proof: interestingstatement A B.
    Proof.
    intros ? ? ? ? homoth1 homoth2 hyp a.
  Fail intermediate path wrong (w (w' (v a))).
```
The message does not point to the problem that argument x appears a second time in the Ltac definition with a different needed type.

Abort. End homot2.

See https://github.com/UniMath/UniMath/blob/master/UniMath/PAdics /frac.v#L27 for a huge Ltac definition in the UniMath library to appreciate the lack of type information.

The UniMath provides some Ltac definitions for general use:

Print Ltac etrans.

no need to explain - rather an abbreviation

```
Set Printing All.
Print Ltac intermediate weq.
```

```
analogous to intermediate_path
Unset Printing All.
Print Ltac show id type.
 Ltac show id type :=       match goal with
         | |- paths _ = ⇒ set (TYPE := ID); simpl in TYPE
                end
```
Not present in any proof in the library, but it can be an excellent tool while trying to prove an equation: it puts the index of the path space into the context. This index is invisible in the notation with an equals sign.

The most useful Ltac definition of UniMath

```
Print Ltac simple rapply.
```
It applies the simple refine tactic with zero up to fifteen unknown arguments.

```
This tactic must not be used in UniMath since a "tactic notation" is favoured:
Foundations/Preamble.v contains the definition
Tactic Notation "use" uconstr(p) := simple rapply p.
```
Use of use:

```
Lemma sumex with use (A: UU) (P Q: A \rightarrow UU):
  (5 x:A, P x \times Q x) \rightarrow (5 x:A, P x) \times 5 x:A, Q x.Proof.
    intro H; induction H as [x H']; induction H' as [H1 H2].
    split.
    - use tpair.
        + assumption.
        + cbn.
```
this is often necessary since use does as little as possible

assumption.

-

to remind the version where the "witness" is given explicitly:

 ∃ x; assumption. Defined.

To conclude: use tpair is the right idiom for an interactive construction of inhabitants of Σ-types. Note that the second generated sub-goal may need cbn to make further tactics applicable.

If the first component of the inhabitant is already at hand, then the "exists"

tactic yields a leaner proof script.

use is not confined to Σ-types. Whenever one would be inclined to start trying to apply a lemma H with a varying number of underscores, use H may be a better option.

There is another recommendable tactic notation that is also by Jason Gross:

```
Tactic Notation "transparent" "assert"
                      "(" ident(name) ":" constr(type) ")" :=
                      simple refine (let name := ( : type) in ).Definition combinatorS curried with transparent assert (A B C: UU):
  (A \rightarrow B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow A \rightarrow C.
Proof.
    intros H1 H2 H3.
    transparent assert (proofofB : B).
    { apply H2; assumption. }
 There is no transparent assert by.
```
Now, proofB is present with the constructed proof of B.

Abort.

To conclude: transparent assert is a replacement for assert if the construction of the assertion is needed in the rest of the proof.

a final word, just on searching the library

SearchPattern searches for the given pattern in what the library gives as *conclusions* of definitions, lemmas, etc., and the current hypotheses.

Search searches in the (full) types of all the library elements (and the current hypotheses). It may provide too many irrelevant result for your question. At least, it will also show all the relevant ones.

List of tactics that were mentioned

```
exact
apply
intro
set
cbn / cbn in (old form: simpl / simpl in)
assumption
intros (with pattern, with wild cards)
```

```
split / split with / ∃
destruct as --- not desirable in UniMath
induction / induction as
admit --- only during proof development
eapply
eexact
refine --- first consider "use" instead
instantiate
unfold / unfold in
intermediate_path (Ltac def.)
rewrite / rewrite <-
change / change in
clear
assert {} / assert by
abstract
etrans (Ltac def.)
intermediate weq (Ltac def.)
show_id_type (Ltac def.)
simple_rapply (Ltac def., not to be used)
use (Ltac notation)
transparent assert (Ltac notation)
```
Index

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