Library lecture_tactics_long_version

Lecture 4: Tactics in UniMath

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This is the extended version of a presentation at the UniMath school 2017 in Birmingham, meant for self-study and for exploring the UniMath library.

The material has been slightly enriched on December 13, 2017, which is one day after the presentation.

Compiles with the command
```
cocq -type-in-type lecture_tactics_long_version.v
```
when placed into the UniMath library

Can be transformed into HTML documentation with the command
```
coqdoc -utf8 lecture_tactics_long_version.v
```

In Coq, one can define concepts by directly giving well-typed terms, but one can also be helped in the construction by the interactive mode.

```
```

**define a concept interactively:**

```
Locate bool.

bool comes from the Coq library
```

```
Definition myfirsttruthvalue: bool.

only the identifier and its type given, not the definiens
```

This opens the interactive mode.

```
The UniMath style guide asks us to start what follows with Proof. in a separate line. In vanilla Coq, this would be optional (it is anyway a "nop").
```

```
Proof.
```
Now we still have to give the term, but we are in interactive mode. If you want to see everything that *involves* booleans, then do

`Search bool`.

If you think there are too many hits and you only want to find library elements that *yield* booleans, then try

`SearchPattern bool`.

If you want to see everything that *involves* booleans, then try

`Search bool`.

`true` does not take an argument, and it is already a term we can take as definiens.

`exact true`.

`exact` is a tactic which takes the term as argument and informs Coq in the proof mode to finish the current goal with that term.

We see in the response buffer: "No more subgoals." Hence, there is nothing more to do, except for leaving the proof mode properly.

`Defined`.

`Defined` instructs Coq to complete the whole interactive construction of a term, verify it and to associate it with the given identifier, here `myfirsttruthvalue`.

`Search bool`.

The new definition appears at the end of the list.

`Print myfirsttruthvalue`.

---

**a more compelling example**

`Definition mysecondtruthvalue: bool.`

`Proof.`

`Search bool`.

`apply negb`.

applies the function `negb` to obtain the required boolean, thus the system has to ask for its argument

`exact myfirsttruthvalue`.

`Defined`.

`Print mysecondtruthvalue`.
mysecondtruthvalue = negb myfirsttruthvalue
    : bool

the definition is "as is", evaluation can be done subsequently:

Eval compute in mysecondtruthvalue.

    = false
    : bool

Again, not much has been gained by the interactive mode.

Definition mythirdtruthvalue : bool.
Proof.
  Search bool.
  apply andb.
apply andb. applies the function andb to obtain the required boolean, thus the
system has to ask for its TWO arguments, one by one

This follows the proof pattern of "backward chaining" that tries to attack goals
instead of building up evidence. In the course of action, more goals can be
generated. The proof effort is over when no more goal remains.

UniMath coding style asks you to use proof structuring syntax, while vanilla
Coq would allow you to write formally verified "spaghetti code".

We tell Coq that we start working on the first subgoal.

- only the "focused" subgoal is now on display
  apply andb.
this again spawns two subgoals
we tell Coq that we start working on the first subgoal
  +

normally, one would not leave the "bullet symbol" isolated in a line
  exact mysecondtruthvalue.
  + exact myfirsttruthvalue.

The response buffer signals:
This subproof is complete, but there are some unfocused goals.
  Focus next goal with bullet -.
The usual "UniMath bullet order" is -, +, *, --, ++, **, ---, +++, ***, and so on (all the ones shown are being used).

Coq does not impose any order, so one can start with, e.g., *****, if need be for the sake of experimenting with a proof.

Reuse of bullets even on one branch is possible by enclosing subproofs in curly braces {}.

Print mythirdtruthvalue.
Eval compute in mythirdtruthvalue.

You only saw the tactics exact and apply at work, and there was no context.

**doing Curry-Howard logic**

Interactive mode is more wide-spread when it comes to carrying out proofs (the command Proof. is reminiscent of that).

Disclaimer: this section has a logical flavour, but the "connectives" are not confined to the world of propositional or predicate logic. In particular, there is no reference to the sort Prop of Coq. Prop is not used at all in UniMath!

On first reading, it is useful to focus on the logical meaning.

Locate "->".

non-dependent product, can be seen as implication

Locate "∅".
Print Empty_set.

an inductive type that has no constructor

Locate "¬".

Require Import UniMath.Foundations.PartA.

Do not write the import statements in the middle of a vernacular file. Here, it is done to show the order of appearance, but this is only for reasons of pedagogy.

Locate "¬".
Print neg.
Negation is not a native concept; it is reduced to implication, as is usual in constructive logic.

Locate "×".
Print dirprod.

non-dependent sum, can be seen as conjunction

Definition combinatorS (A B C : UU): (A × B → C) × (A → B) × A → C.
Proof.

how to infer an implication?
intro Hyp123.
set (Hyp1 := pr1 Hyp123).

This is already a bit of "forward chaining" which is a fact-building process.

set (Hyp23 := pr2 Hyp123).
cbn in Hyp23.

cbn simplifies a goal, and cbn in H does this for hypothesis H; note that simpl has the same high-level description but should better be avoided in new developments.

set (Hyp2 := pr1 Hyp23).
set (Hyp3 := pr2 Hyp23).
cbn in Hyp3.
apply Hyp1.
apply tpair.

could be done with split. as well
- assumption.

instruct Coq to look into the current context
this could be done with exact Hyp3. as well
- apply Hyp2.
  assumption.
Defined.

Print combinatorS.

Local Definition combinatorS_intro_pattern (A B C: UU):
  (A × B → C) × (A → B) × A → C.
Proof.
  intros [Hyp1 [Hyp2 Hyp3]].

deconstruct the hypothesis at the time of introduction; notice that × associates to the right; intros can also introduce multiple hypotheses, see below
  apply Hyp1.
split.
assumption.
- apply Hyp2.
  assumption.

\textbf{Defined.}

\textbf{Print } \texttt{combinatorS\_intro\_pattern}.

\hspace{1em} may look harmless but is not allowed by UniMath coding style

\textbf{Set Printing All.}
\textbf{Print } \texttt{combinatorS\_intro\_pattern}.

\hspace{1em} UniMath coding style forbids the generation of terms that involve \texttt{match} constructs! The UniMath language is a voluntarily limited subset of Coq, and tactics need to be used with care so as to stay within that fragment.

\textbf{Unset Printing All.}

\hspace{1em} However, the two definitions are even convertible:

\textbf{Local Lemma } \texttt{combinatorS\_intro\_pattern\_is\_the\_same}:
\hspace{1em} \texttt{combinatorS = combinatorS\_intro\_pattern}.
\textbf{Proof.}
\hspace{1em} apply \texttt{idpath}.
\textbf{Defined.}

\hspace{1em} another try to make life easier:

\textbf{Local Definition } \texttt{combinatorS\_destruct} \( (A \ B \ C : \texttt{UU}) \): \hspace{1em} \texttt{(A \times B \rightarrow C) \times (A \rightarrow B) \times A \rightarrow C}.
\textbf{Proof.}
\hspace{1em} intro Hyp123.
\hspace{1em} destruct Hyp123 as \([\texttt{Hyp1 Hyp23}]\).
\hspace{1em} deconstruct the hypothesis when needed
\hspace{1em} apply \texttt{Hyp1}.
\hspace{1em} destruct \texttt{Hyp23} as \([\texttt{Hyp2 Hyp3}]\).
\hspace{1em} deconstruct the hypothesis when needed
\hspace{1em} split.
\hspace{1em} - assumption.
\hspace{1em} - apply \texttt{Hyp2}.
\hspace{1em}  assumption.
\textbf{Defined.}

\textbf{Set Printing All.}
\textbf{Print } \texttt{combinatorS\_destruct}.
\textbf{Unset Printing All.}

\hspace{1em} Since we see \texttt{match}, this proof is therefore equally disallowed by UniMath coding style!
Again, the definition is definitionally equal to the first one:

Local Lemma combinatorS_destruct_is_the_same: combinatorS = combinatorS_destruct.
Proof.
  apply idpath.
Defined.

We declared the unwanted definitions and lemmas as Local, so that they would at least not be exported. In the UniMath library, there should be no such definitions at all, not even declared as local.

The way out:

Definition combinatorS_induction (A B C: UU): (A × B → C) × (A → B) × A → C.
Proof.
  intro Hyp123.
  induction Hyp123 as [Hyp1 Hyp23].

wishes to invoke the recursor

  apply Hyp1.
  induction Hyp23 as [Hyp2 Hyp3].

wishes to invoke the recursor

  split.
  - assumption.
  - apply Hyp2.
    assumption.
Defined.

Set Printing All.
Print combinatorS_induction.
Unset Printing All.

Unfortunately, this is not better than before, but it comes from a recent change in the status of Sigma types. They are a record now, in order to profit from "primitive projections". The UniMath team would hope that the Coq developers provide a means of inducing Coq into using the induction principle total2_rect when calling tactic induction on Sigma types and their special case that is pairs.

Notice that even the projections pr1 and pr2 are defined by help of match - for the time being, since this is what happens with non-recursive fields of Coq records.

Definition combinatorS_curried (A B C: UU): (A → B → C) → (A → B) → A → C.
Proof.
  use intro three times or rather intros once; UniMath coding style asks for giving names to all hypotheses that are not already present in the goal.
formula, see also the next definition

intros H1 H2 H3.
apply H1.
- assumption.
- set (proofoB := H2 H3).

set up abbreviations that can make use of the current context; will be considered as an extra element of the context:

assumption.
Defined.

Print combinatorS_curried.

We see that set gives rise to let-expressions that are known from functional programming languages, in other words: the use of set is not a "macro" facility to ease typing.

let-bindings disappear when computing the normal form of a term:

Compute combinatorS_curried.

set can only be used if the term of the desired type is provided, but we can also work interactively as follows:

Definition combinatorS_curried_with_assert (A B C: UU):
  (A → B → C) → (A → B) → A → C.
Proof.
  intros H1 H2 H3.
  we can momentarily forget about our goal and build up knowledge:
    assert (proofoB : B).
the current goal C becomes the second sub-goal, and the new current goal is B

It is not wise to handle this situation by "bullets" since many assertions can appear in a linearly thought argument. It would pretend a tree structure although it would rather be a comb. The proof of the assertion should be packaged by enclosing it in curly braces like so:

{ apply H2.
  assumption.
} 

Now, proofoB is in the context with type B.

apply H1.
- assumption.
- assumption.
Defined.
the wildcard ? for intros

Definition combinatorS_curried_variant (A B C : UU):
  (A → B → C) → (A → B) → ∀ H7:A, C.
Proof.
  intros H1 H2 ?.

a question mark instructs Coq to use the corresponding identifier from the
goal formula

  exact (H1 H7 (H2 H7)).

Defined.

the wildcard _ for intros forgets the respective hypothesis

Locate "Π".

this symbol is harder to type in with Agda input mode: use backslash union
and then choose the right symbol with arrow down key: the symbol might only
appear in the menu to choose from after having hit the arrow down key!

Print coprod.

defined in UniMath preamble as inductive type, can be seen as disjunction

Locate "Π".

company-coq shows the result with universal quantifiers, but that is only the
"prettified" version of "forall" which is a basic syntactic element of the
language of Coq.

Locate "=".

the identity type of UniMath

Print paths.

A word of warning for those who read "Coq in a Hurry": SearchRewrite does
not find equations w.r.t. this notion, only w.r.t. Coq's built-in propositional
equality.

SearchPattern (paths _ _).

Among the search results is pathsinv0l that has idpath in its conclusion.

SearchRewrite idpath.

No result!

How to decompose formulas
In "Coq in a Hurry", Yves Bertot gives recipes for decomposing the usual logical connectives. Crucially, one has to distinguish between decomposition of the goal or decomposition of a hypothesis in the context.

Here, we do it alike.

**Decomposition of goal formulas:**

\( A_1, \ldots, A_n \rightarrow B \): tactic \texttt{intro} or \texttt{intros}

\( \neg A \): idem (negation is defined through implication)

\( \Pi \)-type: idem (implication is a special case of product)

\( \times \): \texttt{apply} \texttt{dirprodpair}, less specifically \texttt{apply tpair} or \texttt{split}

\( \Sigma \)-type: \texttt{use tpair} or \texttt{∃} or \texttt{split with}, see explanations below

\( A \uplus B \): \texttt{apply ii1} or \texttt{apply ii2}, but this constitutes a choice of which way to go

\( A = B \): \texttt{apply idpath}, however this only works when the expressions are convertible

\( \text{nat} \): \texttt{exact 2017}, for example (a logical reading is not useful for this type)

**Decomposition of formula of hypothesis \( H \):**

\( \emptyset \): \texttt{induction H}

This terminates a goal. (It corresponds to \texttt{ex falso quodlibet}.)

There is naturally no recipe for getting rid of \( \emptyset \) in the conclusion. But \texttt{apply fromempty} allows to replace any goal by \( \emptyset \).

\( A_1, \ldots, A_n \rightarrow B \): \texttt{apply H}, but the formula has to fit with the goal

\( \times \): \texttt{induction H as [H1 H2]}

As seen above, this introduces names of hypotheses for the two components.

\( \Sigma \)-type: idem, but rather more asymmetric as \texttt{induction H as [x H']}\n
\( A \uplus B \): \texttt{induction H as [H1 | H2]}

This introduces names for the hypotheses in the two branches.

\( A = B \): \texttt{induction H}

The supposedly equal \( A \) and \( B \) become the same \( A \) in the goal.

This is the least intuitive rule for the non-expert in type theory.
Here, we assume that the hypothesis has the name $n$ which is more idiomatic than $H$, and there is no extra name in the base case, while in the step case, the preceding number is now given the name $n$ and the induction hypothesis is named $IH$.

**Handling unfinished proofs**

In the middle of a proof effort - not in the UniMath library - you can use `admit` to abandon the current goal.

```
Local Lemma badex1 (A: UU): ∅ × (A → A).
Proof.
  split.
  -

  seems difficult in the current context
  admit.

  we continue with decent proof work:
  - intro H.
    assumption.
  Admitted.
```

This is strictly forbidden to commit to UniMath! `admit` allows to pursue the other goals, while `Admitted` makes the lemma available for further proofs.

An alternative to interrupt work on a proof:

```
Proof.
  split.
  -
  Abort.
```

`badex2` is not in the symbol table.

`Abort` is a way of documenting a problem with proving a result. At least, Coq can check the partial proof up to the `Abort` command.

**Working with holes in proofs**

Our previous proofs were particularly clear because the goal formulas and all hypotheses were fully given by the system.
This is the UniMath proof of transitivity of equality.

The salient feature of transitivity is that the intermediate expression cannot be deduced from the equation to be proven.

**Lemma** badex3 \((A \ B \ C \ D : \text{UU}) : ((A \times B) \times (C \times D)) = (A \times (B \times C) \times D)\).

Notice that the outermost parentheses are needed here.

**Proof.**

```
Fail apply pathscomp0.
```

The command has indeed failed with message:

```
Cannot infer the implicit parameter b of pathscomp0 whose type is "Type" in environment:
A, B, C, D : UU
```

(When using the standard setup of UniMath with ProofGeneral, this message appears only when starting emacs at the root of the UniMath library.)

**Fail** announces failure and therefore allows to continue with the interpretation of the vernacular file.

We need to help Coq with the argument \(b\) to \textit{pathscomp0}.

```
apply (pathscomp0 (b := A \times (B \times (C \times D)))).
```

is this not just associativity with third argument \(C \times D\)?

```
SearchPattern(_ \times _).
```

No hope at all - we can only hope for weak equivalence.

**Abort.**

```
SearchPattern(_ = _).
Print weqcomp.
Print weqdirprodasstor.
Print weqdirprodasstol.
Print weqdirprodf.
Print idweq.
```

**Lemma** assocex \((A \ B \ C \ D : \text{UU}) : ((A \times B) \times (C \times D)) \equiv (A \times (B \times C) \times D)\).

**Proof.**

```
Fail apply weqcomp.
eapply weqcomp.
```

\textit{eapply} generates "existential variables" for the expressions it cannot infer from applying a lemma.

The further proof will narrow on those variables and finally make them
disappear - otherwise, the proof is not considered completed.

We recall that on this side, only associativity was missing.

    apply weqdirprodasstor.

The subgoal is now fully given.

The missing link is associativity, but only on the right-hand side of the top $\times$ symbol.

    apply weqdirprodf.
    + apply idweq.
    + apply weqdirprodasstol.

Defined.

Warning: tactic exact does not work if there are existential variables in the goal, but eexact can then be tried.

Lemma sumex (A: UU) (P Q: A → UU):

    (∑ x:A, P x × Q x) → (∑ x:A, P x) × ∑ x:A, Q x.

Proof.

decompose the implication:

    intro H.

decompose the Σ-type:

    induction H as [x H'].

decompose the pair:

    induction H' as [H1 H2].

decompose the pair in the goal

    split.
    - Fail split.

The command has indeed failed with message:

    Unable to find an instance for the variable pr1.

    Fail (apply tpair).

A simple way out, by providing the first component:

    split with x.

$\exists x$ does the same

assumption.
or use `eapply` and create an existential variable:

```coq
  eapply tpair.
  Fail assumption.
```

the assumption $H_2$ does not agree with the goal

```coq
  exact H2.
  Defined.
```

Notice that `eapply tpair` is not used in the UniMath library, since `use tpair` normally comes in handier, see below.

### Warning on existential variables

It may happen that the process of instantiating existential variables is not completed when all goals have been treated.

an example adapted from one by Arnaud Spiwack, ~2007

#### About `unit`.

from the Coq library

```coq
Local Definition P (x:nat) := unit.
```

```coq
Lemma uninstex: unit.
Proof.
  refine ((fun x:P _ ⇒ _) _).
```

`refine` is like `exact`, but one can leave holes with the wildcard ".". This tactic should hardly be needed since most uses in UniMath can be replaced by a use of the "tactic" `use`, see further down on this tactic notation for an Ltac definition.

Still, `refine` can come to rescue in difficult situations, in particular during proof development. Its simpler variant `simple refine` is captured by the `use "tactic"`

- `exact tt`
- `exact tt`

Now, Coq presents a subgoal that pops up from the "shelved goals".

Still, no more "-" bullets can be used.

[ - Error: Wrong bullet - : No more subgoals. ]

Show Existentials.

a natural number is still asked for

Unshelve.
Like this, we can focus on the remaining goal.

exact 0.
Defined.

one can also name the existential variables in refine:

Lemma uninstexnamed: unit.
Proof.
  refine ((fun x:P ?[n] ⇒ _) _).

give a name to the existential variable

  - exact tt.
  - exact tt.

Show Existentials.
Unshelve.
instantiate (n := 0).

more symbols to type but better to grasp
Defined.

a bit more on equational reasoning

Section homot.
A section allows to introduce local variables/parameters that will be bound outside of the section.

Locate "~".

Print homot.
  this is just pointwise equality

Print idfun.
  the identity function

Locate "∘".
Print funcomp.
  plain function composition in diagrammatic order, i.e., first the first argument, then the second argument; the second argument may even have a dependent type

Variables A B: UU.

Definition interestingstatement : UU :=
  ∏ (v w : A → B) (v' w' : B → A),
\[ w \circ w' \sim \text{idfun } B \rightarrow v \circ v \sim \text{idfun } A \rightarrow v' \sim w' \rightarrow v \sim w. \]

Check \((\text{isinjinvmap'}: \text{interestingstatement})\).

Lemma \(\text{ourisinjinvmap'}: \text{interestingstatement}\).
Proof.
  intros.
  is a nop since the formula structure is not analyzed
  unfold \text{interestingstatement}.
  unfold \text{unfolds a definition}
  intros ? ? ? \text{homoth1 homoth2 hyp a}.
  the extra element \text{a} triggers Coq to unfold the formula further; unfold \text{interestingstatement} was there only for illustration!
  we want to use transitivity that is expressed by \text{pathscomp0} and instruct Coq to take a specific intermediate term
  \text{Set Printing All}.
  Print \text{Ltac intermediate_path}.
  reveals that there is an abbreviation for the tactic call we have in mind
  \text{Unset Printing All}.
  \text{intermediate_path } (w (w' (v a))).
  \text{- apply } \text{pathsinv0}.

  apply symmetry of equality
  \text{ unfold homot in homoth1}.
  \text{ unfold funcomp in homoth1}.
  \text{ unfold idfun in homoth1}.
  \text{ apply homoth1}.

  all the \text{unfold} were only for illustration!
  \text{-}
  \text{ Print maponpaths}.
  \text{ apply maponpaths}.
  \text{ unfold homot in hyp}.

  we use the equation in \text{hyp} from right to left, i.e., backwards:
  \text{ rewrite <- hyp}.

  remark: for a forward rewrite, use \text{rewrite} without directional argument
  beautify the current goal:
  \text{ change } ((v' \circ v) a = \text{idfun } A a).

  just for illustration of \text{change} that allows to replace the goal by a convertible expression; also works for hypotheses, e.g.:
  \text{ change } (v' \sim w') \text{ in hyp}. 
since hyp was no longer necessary, we should rather have deleted it:

    clear hyp.
    apply homoth2.
Defined.

Variables v w: A → B.
Variables v' w': B → A.

Eval compute in (ourisinjinvmap' v w v' w').

Opaque ourisinjinvmap'.
Eval compute in (ourisinjinvmap' v w v' w').

Opaque made the definition opaque in the sense that the identifier is still in the symbol table, together with its type, but that it does not evaluate to anything but itself.

If inhabitants of a type are irrelevant (for example if it is known that there is at most one inhabitant, and if one therefore is not interested in computing with that inhabitant), then opaqueness is an asset to make the subsequent proof process lighter.

Opaque can be undone with Transparent:

Transparent ourisinjinvmap'.
Eval compute in (ourisinjinvmap' v w v' w').

Full and irreversible opaqueness is obtained for a construction in interactive mode by completing it with Qed. in place of Defined.

Using Qed. is discouraged by the UniMath style guide. In Coq, most lemmas, theorems, etc. (nearly every assertion in Prop) are made opaque in this way. In UniMath, many lemmas enter subsequent computation, and one should have good reasons for not closing an interactive construction with Defined.

End homot.
Check ourisinjinvmap'.

The section variables A and B are abstracted away after the end of the section - only the relevant ones.

assert is a "chameleon" w.r.t. to opaqueness:

Definition combinatorS_curried_with_assert2 (A B C: UU):
    (A → B → C) → (A → B) → A → C.
Proof.
    intros H1 H2 H3.
    assert (proofofB : B).
    { apply H2.
      assumption.
}
proofofB is just an identifier and not associated to the construction we gave. Hence, the proof is opaque for us.

apply H1.
- assumption.
- assumption.

Defined.
Print combinatorS_curried_with_assert2.

We see that proofofB is there with its definition, so it is transparent.

See much further below for transparent assert that is like assert, but consistently transparent.

**composing tactics**

Up to now, we "composed" tactics in two ways: we gave them sequentially, separated by periods, or we introduced a tree structure through the "bullet" notation. We did not think of these operations as composition of tactics, in particular since we had to trigger each of them separately in interactive mode. However, we can also explicitly compose them, like so:

**Definition** combinatorS_induction_in_one_step (A B C: UU):
  (A × B → C) × (A → B) × A → C.

**Proof.**
  intro Hyp123;
  induction Hyp123 as [Hyp1 Hyp23];
  apply Hyp1;
  induction Hyp23 as [Hyp2 Hyp3];
  split;
  [ assumption
   | apply Hyp2;
     assumption].

Defined.

The sequential composition is written by (infix) semicolon, and the two branches created by split are treated in the |-separated list of arguments to the brackets.

Why would we want to do such compositions? There are at least four good reasons:

(1) We indicate that the intermediate results are irrelevant for someone who executes the script so as to understand how and why the construction / the proof works.

(2) The same tactic (expression) can uniformly treat all sub-goals stemming
from the preceding tactic application, as will be shown next.

**Definition**

```coq
combinatorS_curried_with_assert_in_one_step (A B C : UU):
 (A → B → C) → (A → B) → A → C.
```

**Proof.**

```coq
intros H1 H2 H3;
assert (proofofB : B) by
( apply H2;
  assumption
);
apply H1;
assumption.
Defined.
```

This illustrates the grouping of tactic expressions by parentheses, the variant **assert by** of **assert** used when only one tactic expression forms the proof of the assertion, and also point (2): the last line is simpler than the expected line `[assumption | assumption].`

Why would we want to do such compositions (cont'd)?

(3) We want to capture recurring patterns of construction / proof by tactics into reusable Ltac definitions, see below.

(4) We want to make use of the **abstract** facility, explained now.

**Definition**

```coq
combinatorS_induction_with_abstract (A B C : UU):
 (A × B → C) × (A → B) × A → C.
```

**Proof.**

```coq
intro Hyp123;
induction Hyp123 as [Hyp1 Hyp23];
apply Hyp1;
induction Hyp23 as [Hyp2 Hyp3].
```

Now imagine that the following proof was very complicated but had no computational relevance, i.e., could also be packed into a lemma whose proof would be finished by **Qed**. We can encapsulate it into **abstract**:

```coq
abstract (split;
| assumption
| apply Hyp2;
  assumption).
Defined.
```

**Print** `combinatorS_induction_with_abstract`.

The term features an occurrence of `combinatorS_induction_with_abstract_subproof` that contains the abstracted part; using the latter name is forbidden by the UniMath style guide. Note that **abstract** is used hundreds of times in the UniMath library.


**Ltac language for defining tactics**

Disclaimer: Ltac can more than that, in fact Ltac is the name of the whole tactic language of Coq.

Ltac definitions can associate identifiers for tactics with tactic expressions.

We have already used one such identifier: `intermediate_path` in the Foundations package of UniMath. In file PartA.v, we have the code

```
Ltac intermediate_path x := apply (pathscomp0 (b := x)).
```

```
Print Ltac intermediate_path.
```

```
does not show the formal argument x in the right-hand side. Remedy:
```

```
Set Printing All.
Print Ltac intermediate_path.
Unset Printing All.
```

The problem with these Ltac definitions is that they are barely typed, they behave rather like LaTeX macros.

```
Ltac intermediate_path_wrong x := apply (pathscomp0 (X := x)(b := x)).
```

This definition confounds the type argument X and its element b. The soundness of Coq is not at stake here, but the errors only appear at runtime.

**Section homot2.**

**Variables** A B: UU.

**Lemma** ourisinjinvmap'_failed_proof: interestingstatement A B.

```
Proof.
Fail intermediate_path_wrong (w (w' (v a))).
```

The message does not point to the problem that argument x appears a second time in the Ltac definition with a different needed type.

```
Abort.
End homot2.
```


The UniMath provides some Ltac definitions for general use:

```
PrintLtac etrans.
```

no need to explain - rather an abbreviation

```
Set Printing All.
Print Ltac intermediate_weq.
```
analogous to intermediate_path

Unset Printing All.
Print Ltac show_id_type.

Ltac show_id_type :=
  match goal with
  | |- paths _ _ ⇒ set (TYPE := ID); simpl in TYPE
  end

Not present in any proof in the library, but it can be an excellent tool while trying to prove an equation: it puts the index of the path space into the context. This index is invisible in the notation with an equals sign.

The most useful Ltac definition of UniMath

Print Ltac simple_rapply.

It applies the simple refine tactic with zero up to fifteen unknown arguments.

This tactic must not be used in UniMath since a "tactic notation" is favoured: Foundations/Preamble.v contains the definition Tactic Notation "use" uconstr(p) := simple_rapply p.

Use of use:

Lemma sumex_with_use (A: UU) (P Q: A → UU):
(∑ x:A, P x × Q x) → (∑ x:A, P x) × ∑ x:A, Q x.

Proof.
  intro H; induction H as [x H']; induction H' as [H1 H2].
  split.
  - use tpair.
    + assumption.
    + cbn.

this is often necessary since use does as little as possible
  assumption.
  .

to remind the version where the "witness" is given explicitly:
  ∃ x; assumption.
Defined.

To conclude: use tpair is the right idiom for an interactive construction of inhabitants of Σ-types. Note that the second generated sub-goal may need cbn to make further tactics applicable.

If the first component of the inhabitant is already at hand, then the "exists"
tactic yields a leaner proof script.

use is not confined to Σ-types. Whenever one would be inclined to start trying to apply a lemma $H$ with a varying number of underscores, use $H$ may be a better option.

There is another recommendable tactic notation that is also by Jason Gross:

Tactic Notation "transparent" "assert"
$\text{"(\ident\text{name})\:"}\ \text{constr(\text{type})\:"}$ :=
simple refine (let name := (_ : type) in _).

Definition combinatorS_curried_with_transparent_assert (A B C : UU):
(A → B → C) → (A → B) → A → C.
Proof.
intros H1 H2 H3.
transparent assert (proofofB : B).
{ apply H2; assumption. }

There is no transparent assert by.

Now, proofB is present with the constructed proof of $B$.

Abort.

To conclude: transparent assert is a replacement for assert if the construction of the assertion is needed in the rest of the proof.

**a final word, just on searching the library**

SearchPattern searches for the given pattern in what the library gives as *conclusions* of definitions, lemmas, etc., and the current hypotheses.

Search searches in the (full) types of all the library elements (and the current hypotheses). It may provide too many irrelevant result for your question. At least, it will also show all the relevant ones.

**List of tactics that were mentioned**

exact
apply
intro
set
cbn / cbn in (old form: simpl / simpl in)
assumption
intros (with pattern, with wild cards)
split / split with / \exists
destruct as -- not desirable in UniMath
induction / induction as
admit --- only during proof development
eapply
eexact
refine --- first consider "use" instead
instanitate
unfold / unfold in
intermediate_path (Ltac def.)
rewrite / rewrite <-
change / change in
clear
assert {} / assert by
abstract
etrans (Ltac def.)
intermediate_weq (Ltac def.)
show_id_type (Ltac def.)
simple_rapply (Ltac def., not to be used)
use (Ltac notation)
transparent assert (Ltac notation)